

Computational Fluency

GRADE 2

- Introduce computational strategies for facts to 20 (eg doubles; doubles plus 1)
- Addition and subtraction to 100
- change in quantity (pictorial/symbolic)
- symbolic representation of equality and inequality

GRADE 3

- Emerging computational fluency to 20
- Addition and subtraction to 1000
- Multiplication and division concepts
- one-step addition and subtraction equations with unknown number

GRADE 4

- Developing computational fluency to 20
- Introduce computational strategies for multiplication and division facts to 100
- Addition and subtraction to 10 000
- Multiplication and division of two- or three-digit numbers by one-digit numbers
- Addition and subtraction of decimals to hundredths
- Algebraic relationships among quantities
- One-step equations with an unknown number using all operations

Grade 5

- Extending computational fluency to 20
- Emerging strategies for multiplication and division facts to 100
- Addition and subtraction of whole numbers to 1 000 000
- Multiplication and division to three digits, including division with remainders
- Addition and subtraction of decimals to thousandths
- One-step equations with variables

Grade 6

- Developing strategies for multiplication and division facts to 100
- Order of operations with whole numbers
- Multiplication and division of decimals
- One-step equations with whole number coefficients and solutions

Grade 7

- Extending strategies for multiplication and division facts to 100
- Operations with integers (addition, subtraction, multiplication, division, and order of operations)
- Operations with decimals (addition, subtraction, multiplication, division, and order of operations)
- Two-step equations with whole number coefficients, constants, and solutions

Grade 8

- Operations with fractions (addition, subtraction, multiplication, division, and order of operations)
- Expressions – writing and evaluating using substitution
- Two-step equations with integer coefficients, constants, and solutions

CLASSROOM EXPERIENCES TO SUPPORT COMPUTATIONAL FLUENCY

- Number line routines (e.g. Clothesline Math)
- Number talks
- Interactive read alouds
- Small group instruction
- Math stations
- Collaborative problem-solving
- Critical thinking problem-solving
- Land-based learning opportunities

STAGES OF COMPUTATIONAL FLUENCY

COUNTING

Counts with objects or mentally

Example: $8+4$ make a group of 8 and group of 4 and count to 12

DERIVING

Uses reasoning strategies based on known facts

Provide multiple strategies and students select

Example: $8+4=$ make 10 and then add 2 ($8+2+2$)

Example: $8+4=$ $6+6$

MASTERY

Efficiently produces answers

Example: $8+4=12$ student is able to select a strategy to efficiently produce an answer

ASSESSMENT FOR COMPUTATIONAL FLUENCY

SNAP

Fact Fluency Assessments (Addition and Multiplication)

Observations and Observational Data Collection Sheet

Conferences

SNAP Zoom-Ins

RESOURCES/SUPPORTS FOR MATHEMATICAL COMPUTATIONAL FLUENCY

Math Fact Fluency by Jennifer Bay-Williams

Math Games

Fact Fluency Practice

Small group instruction

Fact Fluency Strategy Progressions

Addition

Multiplication

K	<p>Counting</p> <ul style="list-style-type: none"> one-to-one correspondence conservation cardinality stable order counting sequencing 1-10 linking sets to numerals subitizing 	<p>"Add and Subtract 0, 1, and 2"</p> <p>Examples: 2 more than 5, 1 less than 8, 2 less than 3, 1 more than 7</p>	<p>"Combos of 10"</p> <p>Examples: 10+0, 9+1, 8+2, 7+3, 6+4, 5+5, 4+6, 3+7, 2+8, 1+9, 0+10</p>	<p>"Doubles to 10"</p> <p>Examples: 1+1=2 2+2=4 3+3=6 4+4=8 5+5=10</p>	
Gr. 1	<p>Review, reinforce, and allow practice time for the K strategies, plus →</p> <p>Extend addition fluency strategies to numbers up to 20.</p>	<p>"10+ ___"</p> <p>Examples: 10+6=16 3+10=13 9+10=19 10+1=11</p>	<p>"Doubles to 20"</p> <p>Examples: 6+6=12 7+7=14 8+8=16 9+9=18 10+10=20</p>		
Gr. 2	<p>Review, reinforce, and allow practice time for the K and 1 strategies, plus →</p> <p>Extend addition fluency strategies to two-digit numbers up to 100.</p>	<p>"Making Ten"</p> <p>Example: 7+5= 7+3+2= 10+2=12</p>	<p>"Near Doubles"</p> <p>Example: 7+8= 7+7+1=15</p>	<p>"Skip count by 2s, 5s, and 10s"</p> <p>Examples: From zero: 2, 4, 6, 8, 10, 12... From a multiple: 15, 20, 25, 30, 35... Backward: 80, 70, 60, 50, 40, 30...</p>	
Gr. 3	<p>Review, reinforce, and allow practice time for all strategies from previous grades until students have achieved automaticity with addition fact from 1+1=2 to 10+10=20.</p> <p>Extend addition fluency strategies to multi-digit numbers.</p>	<p>Multiplication Concepts</p> <ul style="list-style-type: none"> Understanding concepts of multiplication (e.g., groups of, arrays, repeated addition) Connecting multiplication to skip-counting. 		<p>"Multiply by 0 and 1"</p> <p>Examples: 1x1=1 1x0=0 2x1=2 0x2=0 1x3=3 8x0=0 4x1=4 0x6=0</p>	
<p>By the end of Grade 3, most students should be able to recall addition facts to 20 (From the BC Curriculum)</p>					
Gr. 4	<p>Review, reinforce, and allow practice time for all addition strategies from previous grades until students have achieved automaticity with addition facts from 1+1=2 to 10+10=20.</p> <p>Extend addition fluency strategies to multi-digit numbers.</p>	<p>Review, reinforce, and allow practice time for Gr. 2 and 3 multiplication strategies, plus →</p>		<p>"Add/Subtract a Group"</p> <p>Examples: 10x5 = 50, so 9x5 = 50-5 = 45</p> <p>2x4 = 8, so 3x4 = 8+4 = 12</p>	
<p>Students should be able to recall the following multiplication facts by the end of Grade 4 (2s, 5s, 10s). (From the BC Curriculum)</p>					
Gr. 5	<p>Review, reinforce, and allow practice time for all strategies from previous grades until students have achieved automaticity with addition facts from 1+1=2 to 10+10=20.</p> <p>Extend addition fluency strategies to multi-digit numbers.</p>	<p>Review, reinforce, and allow practice time for Gr. 2, 3, and 4 strategies, plus →</p>	<p>"Squares"</p> <p>Examples: 1x1=1 2x2=4 3x3=9 4x4=16</p>	<p>"Near Squares"</p> <p>Example: 8x8 = 64, so 9x8 = 64+8 = 72 7x7 = 49, so 6x7 = 49-7 = 42</p>	<p>"Doubling"</p> <p>If you can multiply by 2, then you can double to find your 4s, and double again to find your 8s.</p> <p>Examples: 2x6 = 12 4x6 = 24 8x6 = 48</p>
<p>Students should be able to recall the following multiplication facts by the end of Grade 5 (2s, 3s, 4s, 5s, 10s). (From the BC Curriculum)</p>					
Gr. 6	<p>Review, reinforce, and allow practice time for all strategies from previous grades until students have achieved automaticity with addition facts from 1+1=2 to 10+10=20.</p> <p>Extend addition fluency strategies to multi-digit numbers.</p>	<p>Review, reinforce, and allow practice time for all strategies from previous grades until students have achieved automaticity with multiplication facts from 0x0=0 to 10x10=100.</p> <p>Extend multiplication fluency strategies to multi-digit numbers.</p>			
<p>Students should be able to recall all one-digit by one-digit multiplication facts by the end of Grade 6. (0x0 = 0 to 10x10 = 100)</p>					
Gr. 7	<p>Review, reinforce, and allow practice time for all strategies from previous grades until students have achieved automaticity with addition facts from 1+1=2 to 10+10=20.</p> <p>Extend addition fluency strategies to multi-digit numbers.</p>	<p>Review, reinforce, and allow practice time for all strategies from previous grades until students have achieved automaticity with multiplication facts from 0x0=0 to 10x10=100.</p> <p>Extend multiplication fluency strategies to multi-digit numbers.</p>			

Fact Fluency Games for Strategy Practice

from "Math Fact Fluency"

by Jennifer Bay-Williams and Gina Kling



QR code for game instructions and blackline masters

K	<p>Counting</p> <ul style="list-style-type: none"> one-to-one correspondence conservation cardinality stable order counting sequencing 1-10 linking sets to numerals subitizing 	<p>"Add and Subtract 0, 1, and 2"</p> <ul style="list-style-type: none"> Sleeping Bears Bears Race to 10 Bears Race to 0 Bears Race to Escape 	<p>"Combos of 10"</p> <ul style="list-style-type: none"> 10 Sleeping Bears Go Fish for 10s Erase 	<p>"Doubles to 10"</p> <ul style="list-style-type: none"> Doubles Match-Up Doubles Bingo 	
Gr. 1	<p>Review, reinforce, and allow practice time for the K strategies, plus ➡</p> <p>Extend addition fluency strategies to numbers up to 20.</p>	<p>"10+ ___"</p> <ul style="list-style-type: none"> Square Deal 	<p>"Doubles to 20"</p> <ul style="list-style-type: none"> Doubles Match-Up Doubles Bingo 		
Gr. 2	<p>Review, reinforce, and allow practice time for the K and 1 strategies, plus ➡</p> <p>Extend addition fluency strategies to two-digit numbers up to 100.</p>	<p>"Making Ten"</p> <ul style="list-style-type: none"> Addition Salute Old Mascot Diffy Dozen Concentration Sum War Lucky 13 	<p>"Near Doubles"</p>	<p>"Skip count by 2s, 5s, and 10s"</p> <p>Classroom activities and resources:</p> <ul style="list-style-type: none"> Choral Counting Songs and Chants Counting Collections Hundred Charts and Number Lines 	
Gr. 3	<p>Review, reinforce, and allow practice time for all strategies from previous grades until students have achieved automaticity with addition fact from $1+1=2$ to $10+10=20$.</p> <p>Extend addition fluency strategies to multi-digit numbers.</p>	<p>Multiplication Concepts</p> <ul style="list-style-type: none"> Sticker Book Patterns On the Double Trios Capture the 5 First 		<p>"Multiply by 0 and 1"</p> <ul style="list-style-type: none"> How Low Can you Go? 	
<p>By the end of Grade 3, most students should be able to recall addition facts to 20 (From the BC Curriculum)</p>					
Gr. 4	<p>Review, reinforce, and allow practice time for all addition strategies from previous grades until students have achieved automaticity with addition facts from $1+1=2$ to $10+10=20$.</p> <p>Extend addition fluency strategies to multi-digit numbers.</p>	<p>Review, reinforce, and allow practice time for Gr. 2 and 3 multiplication strategies, plus ➡</p>	<p>"Add/Subtract a Group"</p> <ul style="list-style-type: none"> Multiplication Pathways Strive to Derive Multiplication Salute Fixed Factor War 		
<p>Students should be able to recall the following multiplication facts by the end of Grade 4 (2s, 5s, 10s). (From the BC Curriculum)</p>					
Gr. 5	<p>Review, reinforce, and allow practice time for all strategies from previous grades until students have achieved automaticity with addition facts from $1+1=2$ to $10+10=20$.</p> <p>Extend addition fluency strategies to multi-digit numbers.</p>	<p>Review, reinforce, and allow practice time for Gr. 2, 3, and 4 strategies, plus ➡</p>	<p>"Squares"</p> <ul style="list-style-type: none"> Squares Bingo 	<p>"Near Squares"</p> <ul style="list-style-type: none"> Multiplication Pathways Strive to Derive Multiplication Salute Fixed Factor War 	<p>"Doubling"</p> <ul style="list-style-type: none"> Multiplication Pathways Strive to Derive Multiplication Salute Fixed Factor War
<p>Students should be able to recall the following multiplication facts by the end of Grade 5 (2s, 3s, 4s, 5s, 10s). (From the BC Curriculum)</p>					
Gr. 6	<p>Games to practice all four operations:</p> <ul style="list-style-type: none"> Net Zero Softball Hits Three Dice Take 				
<p>Students should be able to recall all one-digit by one-digit multiplication facts by the end of Grade 6. ($0 \times 0 = 0$ to $10 \times 10 = 100$)</p>					
Gr. 7	<p>Games to practice all four operations:</p> <ul style="list-style-type: none"> Net Zero Softball Hits Three Dice Take 				